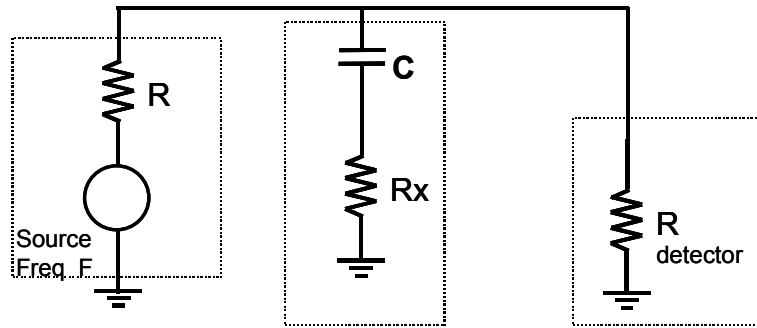


CALCULATION OF THE APPARENT CAPACITANCE (C) IN SHUNT IN A TRANSMISSION CIRCUIT with C and Rx in SERIES



Ici C= capacité
équivalente du
ckt RLC série
F < Frésonnant

$$R := 50$$

$$\text{MHz} := 10^6$$

$$F := 146 \cdot \text{MHz}$$

$$F = 1.46 \times 10^8$$

$$C := 10 \cdot 10^{-12}$$

$$R_x := 0.5$$

**ATT = Linear attenuation in the
transmission ckt, R= source and
detector resistance**

$$ATT = \left| \frac{\frac{R \cdot \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)}{R + \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)}}{\frac{R \cdot \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)}{R + \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)} + R} \right|$$

$$ATT := \left| \frac{\frac{R \cdot \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)}{R + \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)}}{\frac{R \cdot \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)}{R + \left(\frac{1}{j \cdot 2 \cdot \pi \cdot F \cdot C} + R_x \right)} + R} \right|$$

$$ATT = 0.487$$

After simplification:

$$ATT = \left| \frac{1}{2} \cdot \frac{(-i + 2 \cdot R_x \cdot \pi \cdot F \cdot C)}{(-i + 2 \cdot R_x \cdot \pi \cdot F \cdot C + R \cdot \pi \cdot F \cdot C)} \right|$$

solve for C:

$$\left[\begin{array}{c} \frac{1}{2} \cdot \frac{\sqrt{-4 \cdot ATT^2 + 1}}{\left[\sqrt{4 \cdot ATT^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot ATT^2 + R^2 \cdot ATT^2 - R_x^2 \cdot (\pi \cdot F)} \right]} \\ -\frac{1}{2} \cdot \frac{\sqrt{-4 \cdot ATT^2 + 1}}{\left[\sqrt{4 \cdot ATT^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot ATT^2 + R^2 \cdot ATT^2 - R_x^2 \cdot (\pi \cdot F)} \right]} \\ \frac{1}{2} \cdot \frac{\sqrt{-4 \cdot ATT^2 + 1}}{\left[\sqrt{4 \cdot ATT^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot ATT^2 + R^2 \cdot ATT^2 - R_x^2 \cdot (\pi \cdot F)} \right]} \\ -\frac{1}{2} \cdot \frac{\sqrt{-4 \cdot ATT^2 + 1}}{\left[\sqrt{4 \cdot ATT^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot ATT^2 + R^2 \cdot ATT^2 - R_x^2 \cdot (\pi \cdot F)} \right]} \end{array} \right]$$

After simplification:

$$C := \frac{1}{2} \cdot \frac{\sqrt{1 - 4 \cdot ATT^2}}{\left(\sqrt{4 \cdot ATT^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot ATT^2 + R^2 \cdot ATT^2 - R_x^2 \cdot \pi \cdot F} \right)} \quad C = 1 \times 10^{-11}$$

att := 2·ATT **att = atten. in a R - R ohms system (source - det)**

$$att = 0.974$$

$$ATT := \frac{att}{2}$$

$$C := \frac{\sqrt{1 - \text{att}^2}}{\left(\pi \cdot F \cdot \sqrt{4 \cdot \text{att}^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot \text{att}^2 + R^2 \cdot \text{att}^2 - 4 \cdot R_x^2}\right)} \quad C = 1 \times 10^{-11}$$

$$\text{dB} := 20 \cdot \log(\text{att}) \quad \text{att} = 10^{\frac{\text{dB}}{20}} \quad \text{dB} = -0.231 \quad \text{att} = 0.974$$

$$\text{att(dB)} := 10^{\frac{\text{dB}}{20}} \quad \text{att(dB)}^2 = 0.948$$

$$C(\text{dB}) := \frac{\sqrt{1 - \text{att(dB)}^2}}{\pi \cdot F \cdot \sqrt{4 \cdot \text{att(dB)}^2 \cdot R_x^2 + 4 \cdot R \cdot R_x \cdot \text{att(dB)}^2 + R^2 \cdot \text{att(dB)}^2 - 4 \cdot R_x^2}}$$

NOTE that C is the apparent Capacitance

$$C(\text{dB}) = 1 \times 10^{-11}$$

$$\text{dB} := -20, -19.9 \dots -0.1$$

